

The crystal structure of TlAlSiO_4 : The role of inert pairs in exclusion of Tl from silicate minerals

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ABSTRACT

Thallium aluminosilicate, TlAlSiO_4 , synthesized hydrothermally is monoclinic with space group $P2_1/n$ [$a = 5.4095(3)$, $b = 9.4232(7)$, $c = 8.2629(6)$ Å, $\gamma = 90.01(2)^\circ$, $V = 421.20(6)$ Å³, $Z = 4$]. The crystal structure was refined to an R index of 3.8% based on 1852 observed unique reflections. The compound is a unique framework silicate with a topology similar to that of the tridymite structure. The TlO_8 polyhedron resembles a truncated rectangular pyramid, and shares its edges with three adjacent AlO_4 tetrahedra, three SiO_4 tetrahedra, and six TlO_8 polyhedra. Local undercoordination at the Tl position suggested by bond-valence analysis implies that lone-pair electrons are present. The geometrical data indicate that the inert pair causes distortion of the Tl-polyhedron. Polyhedral distortion analysis using the software IVTON places the lone-pair parallel to [010], pointing to the largest base of Tl polyhedron. The rule in the valence shell electron pair repulsion model that a nonbonding pair occupies more space on the “surface” of the central atom than a bonding pair supports the orientation of inert-pair electrons in thallium provided by IVTON. The remarkable structure distortion caused by the inert-pair effect explains the rarity of Tl as a major element in silicate minerals because these cannot accommodate extremely distorted polyhedra. In contrast, about forty species of Tl-sulfide minerals exist because these structures are more flexible. Furthermore this effect probably explains why atoms such as Ge^{2+} , Pb^{2+} , Sn^{2+} , Sb^{3+} , and Bi^{3+} , crystallize not as silicate phases but mainly as sulfide ones in nature.

INTRODUCTION

The low content of thallium in the Earth's crust and its geochemical similarity to potassium and rubidium promote dispersion of this element in endogenic rocks and ore formation (Mason 1966). Recent surveys on the production of subduction-related magmas (Noll et al. 1996) and the origin of Cu-Au porphyry deposits (Kamenetsky et al. 1999) reported efficient mobilization of thallium into arc magma source regions. However, thallium is sequestered in sulfide minerals, e.g., lorandite TlAsS_2 , vrbaitite $\text{Hg}_3\text{Tl}_4\text{Sb}_2\text{As}_8\text{S}_{20}$, and hutchinsonite $(\text{Pb},\text{Tl})_2\text{As}_5\text{S}_9$ (Clark 1993). The only silicate minerals containing major element concentrations of Tl are Tl-bearing ammonioleucites (Nishida et al. 1997) for which the crystal structure was determined by Rietveld refinements of synthetic TlAlSiO_4 (Krogh et al. 1991), and a thallium-leucite pseudomorph after analcime, $\text{TlAlSi}_2\text{O}_6$ (Kyono et al. 1999), which was identified by X-ray powder diffraction.

Even though Tl^+ is similar to K^+ and Rb^+ in chemical properties and ionic size (Shannon 1976), the distinguishing characteristics of Tl depends on an inert-pair effect. The heavier members of Group 13 and 14 develop a valency two less than the normal valency, and distortion along one axis of the M-centered polyhedron often occurs due to the influence exerted by the lone pair (Cotton and Wilkinson 1988; Downs 1993).

Large cations with stereochemically active lone-pair electrons (such as Tl^+ , Pb^{2+} , Sn^{2+} , and Bi^{3+}) have received particular attention owing to their interesting structural features and physical properties (see Gillespie 1972; Moore and Araki 1976; Hawthorne and Groat 1986; Merlino et al. 1993; Cooper and Hawthorne 1995; Cooper et al. 1999 and references therein). The polyhedral distortions that result due to a ns^2 lone pair ($n = 5, 6$) of electrons in the valence shell of the central cation were discussed in detail by Gillespie (1972). Lone-pair effect in the coordination polyhedron in minerals has been studied for about Pb^{2+} , Sb^{3+} , and As^{3+} (e.g., Moore 1988; Moore and Araki 1976; Araki and Moore 1981). This paper determines the crystal structure of TlAlSiO_4 using single-crystal X-ray diffraction and examines if the inert-pair effect causes exclusion of thallium from silicate minerals.

EXPERIMENTAL METHODS

Standard cold-seal hydrothermal techniques were used to synthesize TlAlSiO_4 crystals. About 10 mg of low albite ($\text{Ab}_{98.8}\text{An}_{1.0}$) from Minas Gerais, Brazil was mixed with over 200 mg thallium nitrate and poured into a silver tube 20 mm long and 5 mm diameter). Distilled water was added to give a 70% filling ratio before sealing the tube. The silver tube was heated in an autoclave up to 500 °C for 14 days. Temperature was recorded with Pt/Pt13Rh thermocouples closely adjoining the sample position. Vapor pressure during the synthesis was estimated as 60 MPa. The experiments were stopped by allowing the autoclaves to gradually re-equilibrate to room temperature.

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The morphology of the synthesized samples was examined by optical and scanning electron microscopy (SEM). Each product was polished to a thin section and examined under a high-magnification polarizing microscope. SEM photographs of the synthesized Tl-aluminosilicate show an idiomorphic mineral although these crystals were too small to index the habit.

Chemical compositions were determined using wavelength-dispersion spectroscopy (WDS) on a JEOL superprobe (JXA-8621) operating at 20 kV and 10 nA, with a beam diameter of 10 μ m. Data reduction was carried out using the ZAF procedure. The concentration of Ca was measured using CaSiO₃ as the standard (CaK α_1). The elements Mg, Fe, Ti, Mn, Ni, and Cr were sought, but not detected. Initial analysis of the major elements (Tl, K, Na, Al, Si) was carried out using the synthetic lorandite (TlM α_1) (Berlepsch 1996), microcline (KK α_1), albite (NaK α_1), corundum (AlK α_1) and quartz (SiK α_1) as standards. The accuracy of standard was then tested by cross-analysis with well-characterized minerals. The representative compositions are shown in Table 1. The empirical formula calculated on the basis of four oxygen atoms is (Tl_{0.956}□_{0.044})Al_{0.956}Si_{1.044}O₄, which is close to endmember TlAlSiO₄.

Crystallographic results and discussion

The X-ray powder diffraction patterns were obtained using a RIGAKU diffractometer FR-552 (CuK α_1 radiation, flat graphite monochromator, 2 θ step = 0.02°, scintillation counter, with silicon as an internal standard). The X-ray powder diffraction pattern (Table 2) was indexed on a monoclinic lattice, using the cell parameters from the single crystal data (Table 3). The values of the cell parameters and the XRD pattern are similar to those of the Tl_{1.1}AlSiO₄ (in an ABW-type structure) reported by Krogh et al. (1991). However, the crystal structure of Tl_{1.1}AlSiO₄ which Krogh et al. (1991) determined by Rietveld refinement posed several crystal-chemical problems: (1) The Tl cation on the extra framework site occupies three partially populated positions, (2) their structural formula has an excess 0.1 charge, (3) the positions where the Tl ions are located have curiously irregular surroundings, and (4) the other atoms have abnormal isotropic temperature parameters. These problems prompted redetermination of the crystal structure of TlAlSiO₄.

Structural solution and refinement. X-ray intensity data for TlAlSiO₄ were collected on the Enraf-Nonius CAD-4 diffractometer utilizing graphite-monochromated MoK α radia-

TABLE 1. Chemical analyses

	Theoretical	Measured
SiO ₂	18.58	19.83
Al ₂ O ₃	15.76	15.50
Tl ₂ O	65.66	64.35
Total (wt%)	100.00	99.68
Cations*		
Si	1.000	1.042
Al	1.000	0.959
Tl	1.000	0.956
Total	3.000	2.957

* Based on 4 O atoms.

TABLE 2. X-ray powder diffraction data

<i>h</i>	<i>k</i>	<i>l</i>	<i>I</i> / <i>I</i> ₀	<i>d</i> _{obs} (Å)	<i>d</i> _{calc} (Å)*
0	1	1	8	6.21	6.21
1	1	0	26	4.69	4.69
$\bar{1}$	1	0			
0	0	2	12	4.13	4.13
1	2	1	56	3.264	3.264
$\bar{1}$	2	1			
$\bar{1}$	1	2	100	3.103	3.101
0	3	1	40	2.936	2.936
$\bar{1}$	3	0	18	2.716	2.717
1	3	0			
$\bar{2}$	0	0	22	2.703	2.704
0	$\bar{1}$	3	8	2.644	2.644
2	$\bar{1}$	1	2	2.480	2.480
$\bar{2}$	1	$\bar{1}$			
$\bar{2}$	2	0	14	2.346	2.346
2	2	0			
$\bar{1}$	3	2	6	2.269	2.270
1	3	$\bar{2}$			
2	0	2	12	2.262	2.263
$\bar{1}$	2	3	10	2.177	2.177
1	2	3			
$\bar{1}$	4	1	24	2.090	2.090
1	4	$\bar{1}$			
0	3	$\bar{3}$	24	2.071	2.071
0	0	4	14	2.066	2.066
$\bar{2}$	2	2	10	2.039	2.040
2	2	2			
2	$\bar{3}$	1	24	1.989	1.989
$\bar{2}$	3	1			
0	$\bar{2}$	4	22	1.891	1.892
$\bar{2}$	1	3			
0	5	$\bar{1}$	18	1.837	1.836
$\bar{1}$	5	0	4	1.780	1.780
1	5	0			
$\bar{3}$	1	0	4	1.771	1.771
3	1	0			
1	$\bar{4}$	3	26	1.700	1.700
$\bar{1}$	$\bar{4}$	3			
1	4	3	8	1.650	1.650
3	$\bar{2}$	1			
3	2	1	14	1.644	1.644
$\bar{2}$	3	3			
1	3	$\bar{4}$	10	1.642	1.642
2	0	$\bar{4}$			
3	$\bar{1}$	2	12	1.627	1.628
0	6	0	2	1.570	1.571
3	$\bar{3}$	0	4	1.563	1.564
$\bar{3}$	3	0			
3	3	0	4	1.555	1.556
0	5	$\bar{3}$			
$\bar{2}$	2	4	6	1.550	1.550
2	2	4			
$\bar{2}$	5	1	10	1.520	1.520
2	5	$\bar{1}$			
1	$\bar{2}$	5	10	1.499	1.499
$\bar{1}$	6	1			
1	6	1	6	1.484	1.484
0	$\bar{6}$	2			
0	$\bar{6}$	2	4	1.468	1.468

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TABLE 2—Continued

<i>h</i>	<i>k</i>	<i>l</i>	<i>l</i> / <i>l</i> ₀	<i>d</i> _{obs} (Å)	<i>d</i> _{calc} (Å)*
3	$\bar{3}$	2	6	1.463	1.463
0	3	5			
3	$\bar{2}$	3			
3	2	3	2	1.436	1.437
$\bar{3}$	4	1			
3	4	$\bar{1}$	4	1.411	1.411
0	0	$\bar{6}$			
4	0	0	4	1.352	1.352
$\bar{2}$	5	3			
1	5	$\bar{4}$	6	1.348	1.348
$\bar{3}$	1	4			
0	$\bar{7}$	1	2	1.329	1.329
0	2	$\bar{6}$			
4	$\bar{1}$	1	8	1.323	1.321
1	4	5			
1	$\bar{7}$	0	4	1.313	1.313
3	5	0			
1	7	0	2	1.306	1.306
$\bar{3}$	$\bar{5}$	0			
3	5	0	6	1.303	1.303
1	$\bar{7}$	1			
1	7	$\bar{1}$	6	1.290	1.290
$\bar{2}$	3	5			
$\bar{3}$	4	3	6	1.287	1.271
3	4	$\bar{3}$			
0	6	$\bar{4}$	2	1.251	1.250
$\bar{1}$	7	2			
$\bar{3}$	5	2	6	1.246	1.246
0	5	5			
$\bar{4}$	2	2	4	1.243	1.243
4	2	2			
$\bar{4}$	3	1	6	1.240	1.240
1	3	$\bar{6}$			
0	$\bar{7}$	3	2	1.228	1.228
$\bar{4}$	1	3			
0	$\bar{7}$	3	2	1.210	1.210
$\bar{4}$	1	3			
0	$\bar{7}$	3	2	1.204	1.204
$\bar{4}$	1	3			

* *d*_{calc} based on refined cell parameters: *a* = 5.4090(3), *b* = 9.4236(5) Å, *c* = 8.2644(6) Å, γ = 90.006(6)°, *V* = 421.26(3).

tion for the hemisphere of reciprocal space encompassing *k* > 0. Initial investigation on the diffractometer indicated the presence of only reflections allowed by a *P*-lattice. Intensity data were collected to $\theta = 35^\circ$ with $\omega/2\theta$ scans with a scan angle of $\omega = 1.6^\circ/\text{s}$ plus a correction for dispersion. An electron microprobe analysis, subsequent to measurement of the intensity data, showed that the crystal was homogeneous. Crystal-structure refinements were done with occupancies fixed at the chemical compositions given by electron microprobe results. The experimental details are given in Table 3. An empirical absorption correction was applied using the ψ -scan technique. Data reduction, including background and Lorenz-polarization corrections, was performed with the SDP program (Enraf-Nonius 1983). The program SHELXL-97 (Sheldrick 1997) was used for refinement of the structure in space group *P2₁/n*. Neutral atom scattering factors were used in all refinements. Starting coordinates were taken from the structure of CsLiSiO₄ at −100

TABLE 3. Crystal data

Dimensions	0.10 × 0.12 × 0.07 mm ³
Space group	<i>P2₁/n</i>
Unit cell	<i>a</i> 5.4095(3) Å
	<i>b</i> 9.4232(7) Å
	<i>c</i> 8.2629(6) Å
	γ 90.01(2)°
	<i>V</i> 736.9(2) Å ³
	<i>Z</i> 4
Calculated density	4.959 g/cm ³
μ (MoK α)	1.73 mm ^{−1}
θ limits	≤0.05–30°
Data collected	2052
Unique data	1852
Data > 4 σ_1	1250
Scan type	$\theta/2\theta$
Scan time	≤70 s
<i>R</i> _{merge}	0.054
<i>R</i>	0.038

°C (Asahi and Hasebe 1988), and the structure was refined with a single site model for the Tl position, which successfully converged to *R* = 3.8%. Final positions, displacement parameters, selected interatomic distances are given in Tables 4, 5, and 6.

Description of the structure. The crystal structure of TlAlSiO₄ refined using the CsLiSiO₄ model is isostructural with that of RbAlSiO₄ (Klaska and Jarchow 1975). TlAlSiO₄ exhibits the isotype with the *Icmm*-type framework of RbAlSiO₄, belonging to the series M[AlSiO₄] classified by Liebau (1985). The present compound has a silicate framework similar to that of tridymite, i.e., a framework constructed of zweier chains with all tetrahedra pointing up alternating with zweier chains with all tetrahedra pointing down. The staggered Al–O–Si angles of 174.3° for TlAlSiO₄ are similar to the Li–O–Si angles for CsLiSiO₄, but differ markedly from those of 151.1° in RbAlSiO₄ (Fig. 1). The mean Al–O distance is 1.734 Å, and the mean Si–O distance is 1.611 Å. In spite of the extreme distortion of M-polyhedron, these bond distances indicate a well-ordered framework composed of Al and Si tetrahedra (Jones 1968). Ordering into alternation of SiO₄ and AlO₄ tetrahedra follows Loewenstein's aluminum avoidance rule (Loewenstein 1954).

The present crystal structure, exclusive of the Tl site, is approximately consistent with the structural data for TlAlSiO₄ determined by Krogh et al. (1991). The fundamental building blocks (Hawthorne 1992) in this crystal are the SiAlO₇ pyroanions of an eclipsed type along [100] and [001] and those of a staggered type along [010], polymerization of which leads to formation of the framework silicate. One can view the slabs as consisting of alternating up- and down-tetrahedral chains, parallel to [100] (Fig. 1). Two-dimensional polymerization of those two kinds of pyroanions can be regarded as the six-mem-

TABLE 4. Atomic coordinates and isotropic temperature factors

Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>U</i> _{eq}
Tl	0.7502(1)	0.1891(1)	0.4973(1)	0.0339(3)
Si	0.2503(6)	0.0765(4)	0.2052(4)	0.0233(6)
Al	0.2490(6)	0.4168(3)	0.3082(4)	0.0118(6)
O1	0.2500(22)	0.0657(17)	0.0140(10)	0.0349(27)
O2	0.2447(24)	0.2379(10)	0.2639(19)	0.0546(45)
O3	0.0066(15)	0.9982(9)	0.2788(15)	0.0294(21)
O4	0.4932(13)	−0.0012(9)	0.2824(13)	0.0256(19)

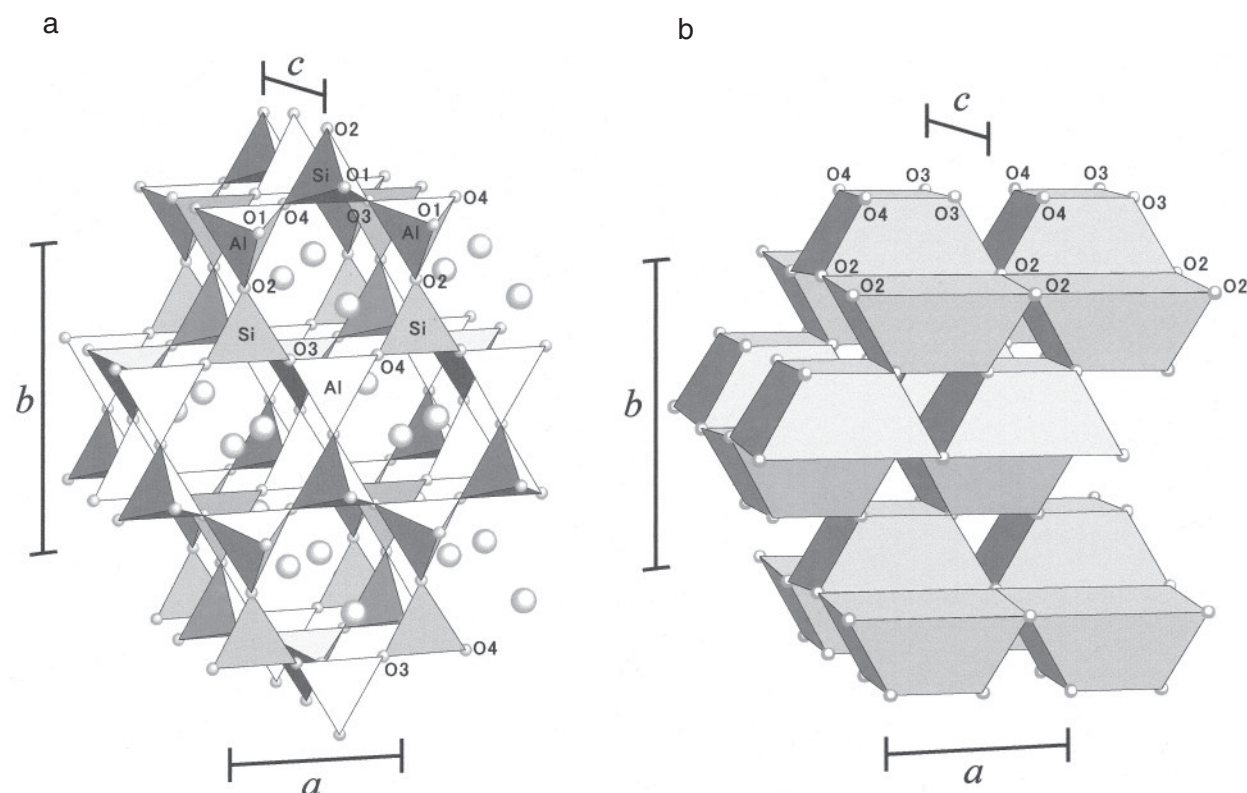


FIGURE 1. (a) Projection of the crystal structure of TlAlSiO_4 parallel to $[001]$ direction. The layers of the six-membered rings approximately perpendicular to $[001]$ belong to the so-called Icmm -type (Liebau 1985). The staggered T_2O_7 pyroanions ($\text{T} = \text{Al}, \text{Si}$) are paralleled to $[010]$ direction, and the eclipsed ones are paralleled to $[001]$ direction. Tl atoms are shown by spheres. (b) The partial structure projected along $[001]$ shown TlO_8 polyhedron shares six edges with Tl polyhedra and six edges with Si and Al tetrahedra.

bered ring layers, and their stacking forms honey-comb-like nets in the (001) planes. Linkage of the fundamental layers vertical to $[001]$ leads to the framework composed of all six-membered rings centered aligned on $[001]$.

The important characteristic of the TlAlSiO_4 structure is the Tl coordination at the M site surrounded by eight O atoms, forming a trapezohedral polyhedron like a truncated rectangular pyramid (Fig. 2). The Tl-O bond lengths are divided into two groups: the short distance group ranges from 2.87 to 2.90 Å (mean 2.88 Å) and the long distance group ranges from 3.34 to 3.57 Å (mean 3.46 Å). This type of asymmetrical coordination is typical for lone-pair-stereoactive Tl^+ (West 1999). The compression along $[010]$ of Tl-polyhedron is a consequence of the stereoactive lone pair of electrons originated from Tl^+ ions.

The stereochemically active lone pair of electrons also manifests itself in the bond lengths, with a considerable increase in the Tl-O2 bond length relative to that of Tl-O3 and Tl-O4. The framework of the crystal structure accommodates chains of edge-shared TlO_8 polyhedra (Fig. 1). The extremely large isotropic temperature factor for O2 suggests hexacoordinated O2; that is the bridging oxygen O2 is in a staggered SiAlO_7 configuration.

The bond valence sums around the total cation sites (Table 7) are in good agreement with the aggregate charge around each anion ($S = 8.08$), which result in the approximate electrostatic cancellation of negative and positive deviations (Brese and O'Keeffe 1991). The sum of the bond valence to the coordinating anions around the Tl site represents a marked deficiency in

TABLE 5. Anisotropic displacement parameters

Atom	U_{11}	U_{22}	U_{33}	U_{12}	U_{13}	U_{23}
Tl	0.0428(5)	0.0260(4)	0.0328(4)	0.0008(3)	-0.0002(2)	0.0010(2)
Si	0.0236(14)	0.0231(14)	0.0231(14)	0.0002(11)	-0.0021(10)	0.0006(11)
Al	0.0106(12)	0.0106(12)	0.0140(12)	0.0021(9)	0.0001(9)	-0.0018(9)
O1	0.0263(45)	0.0611(88)	0.0172(38)	0.0017(48)	-0.0015(28)	-0.0018(36)
O2	0.0713(104)	0.0172(46)	0.0754(115)	0.0167(56)	0.0128(88)	0.0014(61)
O3	0.0274(44)	0.0334(52)	0.0275(52)	-0.0034(37)	0.0020(28)	-0.0044(30)
O4	0.0198(37)	0.0368(52)	0.0202(42)	0.0131(34)	0.0022(23)	0.0012(27)

TABLE 6. Interatomic distances (Å) and interatomic angles (°)

Si-O1	1.583(9)	O1-Si-O2	111.3(8)	Tl-O4'	2.87(1)
Si-O2	1.597(11)	O1-Si-O3	110.1(7)	Tl-O4''	2.87(1)
Si-O3	1.628(9)	O1-Si-O4	111.2(6)	Tl-O3'	2.87(1)
Si-O4	1.634(8)	O2-Si-O3	107.6(6)	Tl-O3''	2.90(1)
Mean	1.611	O2-Si-O4	108.9(6)	Tl-O2'	3.34(1)
		O3-Si-O4	107.6(5)	Tl-O2''	3.36(1)
		Mean	109.5	Tl-O2'''	3.55(1)
				Tl-O2''''	3.57(1)
				Tl-O3'''	3.93(1)
				Tl-O4'''	3.96(1)
				Tl-O4''''	4.00(1)
				Tl-O3''''	4.01(1)
				Mean	3.44
Al-O1	1.709(9)	O1-Al-O2	107.8(6)	Si-O1-Al	170.8(9)
Al-O2	1.725(10)	O1-Al-O3	111.4(6)	Si-O2-Al	174.3(9)
Al-O3	1.745(10)	O1-Al-O4	112.6(5)	Si-O3-Al	133.7(8)
Al-O4	1.753(9)	O2-Al-O3	110.7(6)	Si-O4-Al	131.7(7)
Mean	1.733	O2-Al-O4	109.2(5)	Mean	152.6
		O3-Al-O4	105.1(5)		
		Mean	109.5		

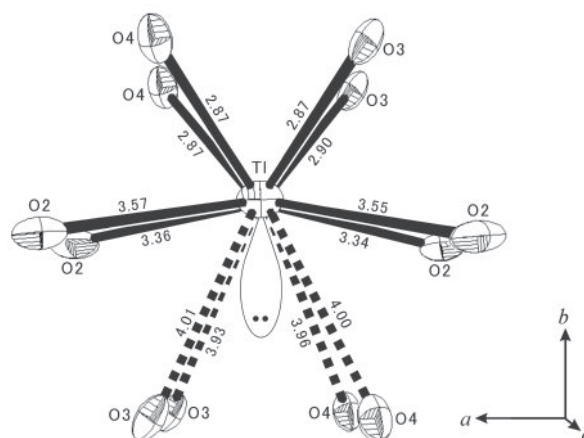
TABLE 7. Bond valence sums

	O1	O2	O3	O4	SV
Si	1.12	1.08	0.99	0.97	4.16
Al	0.85	0.82	0.77	0.76	3.20
Tl	0.02↓ 0.02↓ 0.02↓	0.04 0.04 0.02↓ 0.03→ 0.02→	0.15 0.14	0.15 0.15	0.72
ΣV	2.03	2.02	2.05	2.03	

Note: Bond valences (express in valence units) were calculated from the curve of Brese and O'Keeffe (1991).

electrostatic balance. Both structural distortion of the polyhedron and its deficiency in the bond balance sum are linked to non-bonding electron effects, which are grouped into two types: the *d* electrons in transition metal compounds and the *s*² pair of electrons in compounds of the heavy *p*-block elements in low oxidation states (West 1999). The latter is referred to as so-called the inert-pair effect. Thus the extremely irregular polyhedron of Tl⁺ cation can be explained by the inert-pair effect (Cotton and Wilkinson 1988; Downs 1993). Orientation of the lone-pair electrons of Tl⁺ may account for the larger temperature factor of O2 constituting four apexes of the Tl-polyhedron. Similarly, large temperature factors of O atoms are seen in the Pb-O polyhedra (e.g., Moore et al. 1982, 1989). An abnormality in thermal parameters of ligands is consistent with one of the crystal-chemical characteristics caused by the inert-pair effect.

A comparison of distorted BiMnO₃ with LaMnO₃ (GdFeO₃-type structure), showed that the inert-pair effect of Bi³⁺ tolerates the lower symmetry of the latter structure (Atou et al. 1999). The lowering of the structure symmetry from orthorhombic in the case of RbAlSiO₄ (Klaska and Jarchow 1975) to monoclinic for TlAlSiO₄ is, apparently, caused by the inert-pair effect of the Tl⁺ cation. The observation that compounds having cations with lone-pair electrons are of lower symmetry than the isotopic ones without such cations may hold in general.

**FIGURE 2.** Tl-O coordination environment and bond distances (Å).

Orientation of inert-pair electrons

It is not easy to extract meaningful information about the position of the inert-pair electrons. The sphericity and eccentricity parameters calculated with the computer program IVTON (Balic-Zunic and Vickovic 1996) are listed in Table 8 for the purpose of inferring the position of inert-pair electrons. Our approach arose also from the need to accommodate nonspherical ions into the Brown model used to determine the bond valence sum of Tl cations. The IVTON's parameters are a measure of the degree of deformation of the coordination polyhedra and can provide hints as to site preferences. The sphericity value (*s*) of the KO₉ polyhedra in KAlSiO₄ is the highest (*s* = 0.997), while RbO₈ polyhedra in RbAlSiO₄ show the lowest sphericity (*s* = 0.940) indicative of the most irregular polyhedra in these compounds. The sphericities of any coordination polyhedra are related to the centroid-centered atom distance, namely cation eccentricity, which is the displacement *D* of the central atom from the "best" center of the ligand arrangement. The direction of this displacement is assumed to be opposite to the orientation of the lone pair on this atom (Balic-Zunic and Makovicky 1996). Consequently, large cations in the extraframework sites yield low sphericity and high eccentricity values on account of the low symmetry of their framework structures. It is noteworthy, however, that the crystal structure of TlAlSiO₄ has an extremely large eccentricity value (*d* = 0.779 Å) in spite of the large cation size of Tl. This marked deviation from the centroid implies that the distorted coordination could be caused by the stereochemical activity of the Tl⁺ lone-pair electrons.

The eightfold coordination polyhedra of Tl can be regarded as a truncated rectangular pyramid compressed along [010] (Fig. 1). The compression along [010] is a consequence of the stereoactive lone pair of electrons associated with Tl⁺ ions. The stereochemically active lone pair of electrons also manifests itself in the bond lengths, with a considerable increase in the Tl-O2 bond length relative to those of Tl-O3 and Tl-O4. In the valence shell electron pair repulsion (VSEPR) model (McKenna and McKenna 1984), a nonbonding pair occupies more space on the "surface" of the central atom than a bonding pair (Cot-

TABLE 8. Selected polyhedral parameters for the atoms (Tl, K, Rb)

	CN	V (Å ³)	r (Å)	d (Å)	s	Reference
TlAlSiO ₄	8	37.43	3.414	0.779	0.986	This study
RbAlSiO ₄	8	43.47	3.171	0.067	0.940	Klaska and Jarchow (1975)
KAlSiO ₄	9	46.66	2.968	0.008	0.997	Dollase and Freeborn (1977)

Notes: CN = coordination number; V = Volumes of coordination polyhedron; r = mean distance from centroid to ligands; d = centroid-central atom distance; s = sphericity of coordination polyhedron.

ton and Wilkinson 1988). The IVTON calculations allow us to expose the difference in eccentricity between the polyhedra of an eightfold-coordination and a 12-fold one (Fig. 2), where their apexes are oxygen atoms. The latter eccentricity underscores the validity of the VSEPR model for the lone-pair electrons. Addition of these two IVTON and VSEPR constraints to thermal parameters of the bridging O2 in the staggered SiAlO₇ pyroanions orientated and stacked along [010] bears witness to the space which the non-bonding pair of electrons takes up. This [010] orientation of the Tl-lone pair electrons gives rise to a novel framework for TlAlSiO₄. To reduce steric repulsion between the lone pairs of adjacent Tl ions in the edge-shared eightfold-coordinated blocks, the ions adopt a zigzag arrangement along [001], namely the [001] tetrahedral chain that a Tl polyhedron pointing up continues to alternate with that pointing down. The similar zigzag arrangement of unusually distorted polyhedra due to the tendency of ns² lone pair is exemplified in the K₂Gd₂Sb₂Se₉ compound by the zigzag arrangement of the Sb atoms caused by the steric requirements of the 5s² lone pair of adjacent Sb ions in the edge-shared octahedral blocks (Choi et al. 1999).

Abnormal coordination of thallium ions: Inert-pair effect

One mystery still left to be clarified about Tl⁺ is the necessity for distortion of the polyhedra due to the inert-pair effect: in cases where Tl has the same coordination numbers, there is greater polyhedral distortion for silicates than for sulfides (Kyono et al. 1999). TlAlSiO₄ exhibits a framework structure accommodating an extremely distorted TlO₈ polyhedron (Fig. 2) with the Tl-O bond lengths ranging from 2.87 to 3.57 Å (spread of 0.70 Å), whereas the framework of RbAlSiO₄ contains RbO₁₁ polyhedra with the Rb-O bond lengths ranging from 2.910 to 3.537 Å (Klaska and Jarchow 1975). In thallium borate TlB₃O₅, there are unique polyhedra where six O atoms are around Tl⁺ at distances between 2.662 and 3.198 Å (spread of 0.536 Å) (Touboul et al. 1997). This Tl-polyhedron is significantly different from that of Cs⁺ in CsB₃O₅, with Cs-O distances between 3.030 and 3.342 Å (spread of 0.312 Å) (Krong-Moe 1974), even though Cs⁺ has a larger ionic radius than Tl⁺ (Shannon 1976). The greater distortion of the Tl-polyhedron in TlAlSiO₄ is typical of Tl-O polyhedra in crystal structures (Wells 1987). In thallium sulfides or thallium sulfates, however, the inert-pair effect becomes very little. For instance, the Tl-S distances vary between 3.211 and 3.373 Å (spread of 0.162 Å) in edenharterite, PbTlAs₅S₆ (Berlepsch 1996), and the Tl-O(OH) distances between 2.937 and 3.095 Å (spread of 0.158 Å) in dorallcharite, (Tl,K)Fe₃³⁺(SO₄)₂(OH)₆ (Zunic et al. 1994). Despite the presence of a lone electron pair, there are more uniform distributions of the Tl-S or Tl-O(OH) distances in the Tl polyhedra. Moreover, thallium is more electronega-

tive than the alkali metals and tends to form compounds with polarizable anions, as does silver (Deubener et al. 1991). The difference in the electronegativities of Tl (1.8) and S (2.5) or O (3.5) indicates the low ionicity of Tl-S bond relative to Tl-O. Hence, in silicates or borates the polyhedral distortion due to the inert-pair effect is pronounced at Tl sites, while in sulfides or sulfates it is minimized.

The inert-pair effect of Tl⁺ cation in the TlAlSiO₄ structure may be increased because the bridging anion of the Si-O-Si dimer in the feldspar framework exhibits only one localized nonbonded lone electron pair (Gibbs et al. 1998), and the chemical bonds between Tl⁺ and its surrounding O²⁻ are underlied by the hard-soft acid-base (HSAB) principle (Douglas et al. 1994). A hard acid prefers to combine with a hard base, and a soft acid prefers to combine with a soft base. Inasmuch as soft acid-base interactions involve significant polarization (covalence), soft acids (e.g., Ag⁺, Hg⁺, Tl⁺) and hard bases (e.g., F⁻, OH⁻, O²⁻) bind electrons tightly, and thus the electron clouds cannot be easily distorted or polarized. This behavior causes extreme distortion of TlO₈ polyhedra, as in TlAlSiO₄. Therefore, both the reciprocal interactions between lone-pair electrons due to an inert-pair effect and localized nonbonded lone electron pairs present in the bridging O atoms leads to our interpretation that it may be highly characteristic of Tl⁺ cations to have extremely distorted oxypolyhedra in the polymerized aluminosilicates.

Geological implications

Prior to this study, little was known about factors that give rise to the rare occurrence of thallium-silicate minerals in nature. This study shows that TlAlSiO₄ has extremely distorted polyhedra caused by the inert-pair effect of Tl atoms, and it is likely that the effect is manifested to a greater degree in silicates as opposed to sulfides. The inert-pair effect is generally known for Ge²⁺, Pb²⁺, Sb³⁺, Sn²⁺, and Bi³⁺ (Cotton and Wilkinson 1988), and many minerals having these cations as major constituents crystallize as sulfides in nature, e.g., briartite Cu₂FeGeS₄ (Wintenberger 1979), galena PbS (Noda et al. 1987), stibnite Sb₂S₃ (Bayliss and Nowacki 1972), stannite Cu₂FeSnS₄ (Hall et al. 1978), and pavonite AgBi₃S₅ (Makovicky et al. 1977).

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